

Railroad Ballast Particle Breakage with Unique Laboratory Test Method

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Abstract: This paper demonstrates the results in the research topic of the railway ballast particles' breakage test with unique laboratory test. The most railway lines in the world have so called traditional superstructure (ballasted tracks). In the past few years there were a lot of railway rehabilitation projects in Hungary, as well as abroad. Nowadays cannot be expected that there is enough quantity of railway ballast in adequate quality, because of the modifications and restrictions in the related regulations in Hungary since 2010. In Hungary there are only a few quarries which are able to ensure adequate railway ballast material for construction and maintenance projects for speed values between 120 and 160 km/h. This may cause supply and quality risk in production of railway ballast. The authors' research's main goal is to be able to simulate the stress-strain effect of ballast particles in real and objective way in laboratory conditions as well as in discrete element modelling.

Keywords: ballast, breakage, laboratory test, railway, degradation

1. Introduction

An article was published [1] in 2015 with results of an R&D on individual breakage test method in laboratory related to railway ballast. Since that several other publication was published in this topic [2-6]. The authors would like to supplement that documents with actual, up-to date outcomes.

The rock physical suitability of railway ballast materials is determined by laboratory tests in in the EU, formulated in the same product standard.

There are two types of standardized tests in the aspect of rock physic characteristics of railway ballast:

- Micro-Deval abrasion test according to MSZ EN 1097-1:2012 [7],
- Los Angeles abrasion test in accordance with MSZ EN 1097-2:2010 [8].

These are determined in the MSZ EN 13450:2003 product standard [9].

These two test types are absolutely suitable for satisfy defining the abrasion characteristics of a given aggregate sample and for ensuring the production stability in the quarries and these are indispensable to guarantee the required quality and to ensure the checking of the quality level in case of ready constructed railway tracks. However, it's not suitable for modelling the railway loads (i.e. loads from vehicles and other effects) in a real way.

The authors worked out an individual laboratory test method [1, 3], because other test methods can't consider the abrasion and breakage (real particle degradation) due to dynamic force and vibration.

The results of the unique laboratory tests with the required limits in standards are compared with the related regulation of MÁV (Hungarian Railways) [10]. Required time intervals of ballast screening are able to be calculated according to laboratory test results.

It is known that No. MÁV 102345/1995. PHMSZ in accordance with the decree [10], the "Constructions for superstructure facilities and quality standards for bedding instruction" has been tightened on the basis of the 4th amendement [10], which came into force in January 2010. According to the 3rd amendement of 2008, there was a (positive) tolerance range for the Los Angeles breakdown and the Micro-Deval wear, which was deleted in 4th amendement. The values for the speed categories are also partially have changed, usually tightened (*see Table 1. and Table 2.*).

strength	LA _{RB}				
requirement	2008 - 2009		from 2010		
allowed speed (km/h)	requirement	allowed difference	requirement	allowed difference	
V > 160	16	+2 (negative is not limited)	16	-	
$160 \ge V > 120$	16	+4 (negative is not limited)	16	-	
$120 \ge V \ge 80$	16	+4 (negative is not limited)	16	-	
$80 > V \ge 40$	24	+4 (negative is not limited)	20	-	
V < 40	24	+4 (negative is not limited)	24	-	

Table 1. Requirements to LA_{RB} values [10]

Table 2. Requirements to M _{DE} RB values [10])]
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strength	M _{DE} RB				
requirement	2008 - 2009		from 2010		
allowed speed (km/h)	requirement	allowed difference	requirement	allowed difference	
V > 160	11	+2 (negative is not limited)	11	-	
$160 \ge V > 120$	11	+4 (negative is not limited)	11	-	
$120 \geq V \geq 80$	11	+4 (negative is not limited)	15	-	
$80 > V \ge 40$	15	+4 (negative is not limited)	15	-	
V < 40	15	+4 (negative is not limited)	15	-	

2. History of the research

The research topic has prestigious international literature and sources. Foreign researchers dealt with different areas and they worked out different methods as follows:

- laboratory tests [11, 12, 13, 14, 15, 16, 17, 18, 19]
- finite element modelling (FEM) [13],
- discrete element modelling (DEM) and/or 3D particle generation [19, 20],
- in-situ tests in railway tracks [21].

The researchers worked out several special parameters, constants and indexes that helped the progression of the research (e.g. Marshal, Hardin, Lee and Farhoomand breakages, BBI index, B_R index, etc.).

An international literature review was carried out by the authors and from the results the following main themes and methods were taken into consideration:

- searching of relationship between cohesion as well as inner friction anger, railway ballast aggregate abrasion, water permeability of material and its layer [16];
- definition of relationship between Particle Size Distribution (PSD) and particle degradation phenomenon of ballast aggregate, as well as definition of better PSD for real loadings [15, 16];
- research of 'angularity breakage' phenomena [18];
- DEM models were validated and DEM generations method of much more realistic particle shapes was investigated [22];
- measurement of railway ballast's breakage, implementation of laboratory and field tests with and without geosynthetic inclusions [13, 14, 15, 21];
- research of ballast particle breakage due to tie tamping [11, 12];
- investigation of ballast with glued technique [17].

The authors collected several significant results at the international literature review which can be read in the previous publication [4].

3. The laboratory test's procedure and parameters

The base of the procedure is a special laboratory dynamic actuator The laboratory test method was developed as a part of an R&D financed by Colas Északkő Ltd. and a report more publications – that were written in this topic [1, 2, 3, 4, 5, 6].

In 2017 and 2018 the testing and evaluating method was accomplished by specify more precise deterioration process, considering only determined particle fraction, etc. The authors used the following parameters during measurements and evaluation:

- two different types of railway ballast samples from andesite material and from different quarries
- the specimens are in accordance with MSZ EN 13450:2003 [9], A type, 31,5/50 mm, the authors received from Colas Északkő Ltd.
- the specimens have the following stone physic parameters (laboratory test were done by accredited laboratory of Colas Északkő Ltd.):
 - o sample No. 1: $LA_{RB} = 19\%$, $M_{DE}RB = 17\%$;
 - sample No. 2: $LA_{RB} = 16\%$, $M_{DE}RB = 4\%$;
- dynamic tests with pulsator in different cycles (i.e. until 0.1, 0.2, 0.5, 1.0, 1.5, 3.0 and 5.0 million cycles), in every test with only fresh ballast material with particle fraction *d*≥22.4 mm (before pulsating *d*<22.4 mm particles were screened out and they were not put back), where *d* is the size of the particle; in the 2014 series of measurements, the particle sizes below 22.4 mm were left in the tests, this was the reason why it is not possible to compare the current measurement results with the old ones;
- determination of PSD curves with screening related to sub-samples Before Pulsating (BP) test;
- determination of PSD curves with screening related to sub-samples After Pulsating (AP) test.

3.1. Presentation of the individual fatigue laboratory test

The individual laboratory testing method is a dynamic pulsating test for that the six lower frames of a 10-level steel shear box were used [1]. Frames were fixes together with steel metric screws. They prevent the horizontal relative displacements. The shear box including some steel rolls which were not fixed to the down side of the bottom frame.

The built-up layer structure is the following (see Table 3).

Table 3. The built-up layer structure



The samples (railway ballast) were put in the middle of the shear box into the 0.46×0.46 m area and 0.30 m high space where wooden sleepers are around. The structure can be seen in *Table 1*. Reducing and excluding wall effect the inner sides of wooden sleepers were covered with 1200 g/m² mass geotextile layers (where stone and wooden sleepers would interact). A loading plate from steel (size: 46×42 cm and D=300 mm circular steel plate) were put onto ballast samples to be able to achieve uniform load distribution.

The assembly without loading plates can be seen in Figures 1-5.



Figure 1. The 10-cm-thick-layer sand on the XPS layer



Figure 2. The high strength geotextilie on the sand layer



Figure 3. The wooden sleepers in the shear box



Figure 4. The geotextilie among the wooden sleepers



Figure 5. The sample of ballast material in place

Laboratory measurements were executed with dynamic actuator in previously defined loading cycles. Laboratory test parameters (frequency, load values, etc.) were published in [1, 3] papers in detailed formats, they are not written here due to limited space. After pulsating tests PSD (particle size distribution) data sets were determined (measured) beside them several parameters (see below) were calculated [1, 2, 3]:

- $F_V(\%)$ (see eqs. (1-5));
- *BBI* (see eq. (6));
- B_R , (B_R is a parameter is similar to BBI, but it considers different areas in PSD [24]);
- *d*<22.4 *mm* in mass percentage;

- *d*<0.5 *mm* in mass percentage;
- *d*<0.063 *mm* in mass percentage;
- d₆₀/d₁₀ ratio (where d₆₀ is the particle size related to 60% in PSD curve, d₁₀ is the particle size related to 10% in PSD curve, and d₆₀/d₁₀ ratio means the ratio of (d₆₀/d₁₀)_{AP}/(d₆₀/d₁₀)_{BP};
- $C_C \ ratio$ (where $C_C = d_{30}^2 / (d_{60} \times d_{10})$, d_{30} is the particle size related to 30% in PSD curve, and $C_C \ ratio$ means the ratio of $(C_C)_{AP} / (C_C)_{BP}$;
- *M ratio* (where *M* is a special shape factor of PSD curve of railway ballast [25], and *M ratio* means the ratio of M_{AP}/M_{BP} ;
- λ *ratio* (where λ is a special shape factor of PSD curve of railway ballast that considers standard ballast PSD, as well [25], and λ *ratio* means the ratio of λ_{AP}/λ_{BP}).

Calculations of F_V and BBI parameters have to be explained, eqs. (1-6) give the meaning of these parameters [1, 2, 3, 14, 15, 26].

$$F_V = 0.4 \cdot F_{19} + 0.3 \cdot F_{6.7} + 0.2 \cdot F_{1.18} + 0.4 \cdot F_{0.15}, \quad (1)$$

$$F_{19} = \frac{D_{19}}{100} \cdot 27,\tag{2}$$

$$F_{6.7} = \frac{D_{6.7}}{100} \cdot 18,\tag{3}$$

$$F_{1.18} = \frac{D_{1.18}}{100} \cdot 11.5,\tag{4}$$

$$F_{0.15} = \frac{D_{0.15}}{100} \cdot 5.5,\tag{5}$$

where "D" is the fallen mass percentage through the given diameter sieve.

$$BBI = \frac{A}{A+B},$$
 (6)

where A is the area between the initial and final PSD curves [14, 15], B is the area between the arbitrary boundary of maximum breakage line and final PSD curve [14, 15].

The authors computed the required time intervals of ballast screening with the help of deterioration process obtained from parameters above. The prescribed values from standards were also computed.

4. Recent results

The two ballast samples tested until 5-5 million cycles with dynamic pulsating laboratory test in more phases. The authors calculated the necessary parameters from PSD data sets are plotted in diagrams as a function of pulsating cycles in *Figure 6-25*.

Following diagrams show the parameters in the consideration of the maximum 5-5 million loading cycles, as well as the results in *Figure 6-25*.



Figure 6. Results of the individual laboratory test $-F_V(\%)$ as a function of number of loading cycles; with power regression functions



Figure 7. Results of the individual laboratory test $-F_V(\%)$ as a function of number of loading cycles; with linear regression functions



Figure 8. Results of the individual laboratory test – BBI as a function of number of loading cycles; with power regression functions



Figure 9. Results of the individual laboratory test – BBI as a function of number of loading cycles; with linear regression functions



Figure 10. Results of the individual laboratory test $-B_R$ as a function of number of loading cycles; with power regression functions



Figure 11. Results of the individual laboratory test $-B_R$ as a function of number of loading cycles; with linear regression functions



Figure 12. Results of the individual laboratory test -d < 22.4 mm (%) as a function of number of loading cycles; with power regression functions



Figure 13. Results of the individual laboratory test -d < 22.4 mm (%) as a function of number of loading cycles; with linear regression functions



Figure 14. Results of the individual laboratory test – d<0.5 mm (%) as a function of number of loading cycles; with power regression functions



Figure 15. Results of the individual laboratory test – d<0.5 mm (%) as a function of number of loading cycles; with linear regression functions



Figure 16. Results of the individual laboratory test -d < 0.063 mm (%) as a function of number of loading cycles; with power and linear regression functions



Figure 17. Results of the individual laboratory test - d < 0.063 mm (%) as a function of number of loading cycles; with linear regression functions



Figure 18. Results of the individual laboratory test $- d_{60}/d_{10}$ ratio as a function of number of loading cycles; with power regression functions



Figure 19. Results of the individual laboratory test $- d_{60}/d_{10}$ ratio as a function of number of loading cycles; with linear regression functions



Figure 20. Results of the individual laboratory test $-C_C$ ratio as a function of number of loading cycles; with power regression functions



Figure 21. Results of the individual laboratory test $-C_C$ ratio as a function of number of loading cycles; with linear regression functions



Figure 22. Results of the individual laboratory test – M ratio as a function of number of loading cycles; with power regression functions



Figure 23. Results of the individual laboratory test – M ratio as a function of number of loading cycles; with linear regression functions



Figure 24. Results of the individual laboratory test – λ ratio as a function of number of loading cycles; with power regression functions



Figure 25. Results of the individual laboratory test – λ ratio as a function of number of loading cycles; with linear regression functions

There are significant correlations in four calculated parameters from ten cases (linear and power regression functions, independent variable are the number of loading cycles):

 F_V : the parameter recommended by the South African Railways [26]. This indicates the necessity of ballast screening. It can be approximated by power regression function of the number of loading cycles (see Figure 6). When it reaches the 5 million loading cycles, the F_V equals are 5.0 and 6.5%. It is an interesting fact that better ballast sample deteriorates faster than the less good ballast sample. This means the considering stone physics attribution sample #2 has lower LA_{RB} and M_{DE}RB values then sample #1. Ballast screening has to be executed if F_V =80% according to literature [26]. In case power regression functions are considered and number of loading cycles is calculated related to $F_V=80\%$, they are 2.1×10^{16} cycles and 2.24×10^{11} cycles (for sample #1 and sample #2, respectively). These values means 8-10 million loading cycles (throughrolled axles) what are unrealistic high. On Kelenföld-Hegyeshalom state border, No. 1 railway mainline in Hungary the loading is approximately 15 million MGT/year, that is 666.667 axles/year - and it taking into consideration the common used time interval of ballast screening (12-15

years) [26]. In this aspect, results obtained from analysis of F_V parameter and its extrapolation cannot be used dependably.

- BBI: the parameter introduced by Indaratna and Lackenby [14, 15] to be able to calculate and assess the changing of PSD of tested samples and their quality. For calculation the BBI index, the authors have to determine the BP and AP values and with these the PSD curves. There is linear regression correlation between BBI and number of loading cycles (see Figure 9), but it has to be mentioned that in case of sample #1 the R2 coefficient is negative. The negative value mathematical means that the given correlation is worse than the y has constant function. It has to be mentioned that BBI(0)=0 was a border condition. If measured data before 1.0 million loading cycle are analysed they are outliers from the defined linear trend. The measurements are needed to repeat, because of the ability to evaluate fair. BBI values are approximately 0.15% and 0.20% at 5 million loading cycles related to tested ballast material samples. It is interesting too that sample #2 has higher tangent (steeper slope) than sample #1 (see F_V , too). The authors neglect the negative R_2 value, because after 1.5 million loading cycles the given linear trend can be assumed). According to the literature [14, 15], if the BBI=1.0, ballast screening is needed. In case number of loading cycles related to both samples are computed in the accordance BBI=1.0, the results are 31.45 and 25.84 million cycles (for sample #1 and #2, respectively). That means approximately 47-year and 39-year time intervals.
- B_R : this is a similar parameter with the BBI parameter, because reference area is calculated like in case of BBI [24]. In this way the linear regression functions and correlation are very close to BBI's results. There is no technical recommendation for ballast screening related to B_R (see *Figures* 10-11).
- d < 22,4 mm is mass percentage: between the *d* parameter and the number of loading cycles there are power regression relationships (*see Figures* 12-13). This parameter's values are approximately 3.0% and 4.25%, if the number of loading cycles is 5×10^6 related to investigate andesite materials. This is mentioned above, but it is a surprising fact again that the sample #2 with better properties has quicker deterioration than sample #1. According to literature [26] ballast screening has to be done if d < 22.4mm is equal or higher than 30%. In case numbers of loading cycles has to be determined they are the following: 2.17×10^{12} and 3.27×10^{10} cycles (for sample #1 and #2, respectively) that are unrealistic values.
- d<0,5 mm is mass percentage: between the d parameter and the number of loading cycles there is no power and linear regression relationship (see Figures 14-15).

- *d*<0.063 *mm is mass percentage*: between the *d* parameter and the number of loading cycles there is no power and linear regression relationship (*see Figures 16-17*).
- d_{60}/d_{10} ratio parameter: between the d_{60}/d_{10} ratio parameter and the number of loading cycles there is no power and linear regression relationship (see Figures 18-19).
- *C_c ratio parameter:* between the *C_c ratio parameter* and the number of loading cycles there is no power and linear regression relationship (*see Figures 20-21*).
- M and λ ratio parameters: these parameters can be specified by linear regression function (*see Figures 22-25*). The tangent of regression function is higher in case of sample #2 than sample #1 (the sign is positive for sample #2 and negative for sample #1). The authors analysed the data more detailed and determined that there is an outlier point in case of sample #2 (at 5 million cycles, both M and λ ratio parameters), the reason of it has to be searched by additional tests.

5. Summary, outlook, future scope

There are significant correlations in case of just four from the nine calculates parameters if the independent variable is the number of loading cycles (linear or power). With the other five parameters we did not achieve any results.

The authors considered the following derelictions related to calculation of time intervals between ballast screenings:

- in the whole ballast cross section comparable amount of breakage is not formulated as the one that was measured in referred laboratory tests (e.g. there is hardly no breakage in the ballast shoulder, etc.);
- machine-made and/or manual tamping occurred breakage;
- only 225 kN axle load was taken into consideration (it is true for freight trains, for passenger trains about 180 kN value would be more realistic);
- other ballast polluting effects (e.g. dust, concrete sleeper abrasion, breakage, in case of water pockets the increase of fine particle content in the ballast bed because of evolving pumping effect due to repeated dynamic load, etc.);
- deterioration effect accelerated by substructure or superstructure defect;
- effects of other dynamic loadings (e.g. welts, rail joints, turnout frogs [27, 28, 29, 30, 31, 32]);
- effects of track geometry and its degradation [33].

This paper introduced the research problem related to railway ballast particle degradation. The publication sentenced that the individual laboratory testing method can be suitable for measure and evaluate ballast materials' breakage using dynamic

pulsator. This procedure can give opportunity that ballast samples are tested in more realistic circumstances than during standardized abrasion tests.

The authors summarized the up-to-date results of exhausting international literature in this research topic; they made a remarkable successes related to ballast particle breakage.

It can be stated that better ballast material (in the aspect of stone physics) does not deteriorate slower than the worse one. Parameters that are used internationally were calculated, as well as the deterioration process was approximated linear or power regression functions related to all parameters.

The authors defined the time interval values of ballast screening based on technical prescriptions, standards and handbooks. This calculation could be done for F_V , *BBI* and *d*<22.4 parameters. Only *BBI* gave nearly acceptable results, in case of the other parameters the results are not realistic, they can't be accepted.

In some cases, additional control measurements have to be accomplished in the laboratory to be able to assess the measured data.

The authors would like to search the correlation (relationship) – as future scope – between standardized parameters (Los Angeles and Micro-Deval abrasions), the prognosticated time interval between ballast screening, as well as the results from their laboratory tests. In the beginning of 2019 a modified layer structure will be considered because the extruded polystyrol sheets were significantly deformed during the dynamic tests. A stiffer and harder layer (e.g. granular protection layer or steel/concrete plate, maybe) can be modified laboratory tests' results in better way, as well as difference between substructure circumstances with XPS sheets and stiffer layer is able to be published.

The time requirement of newly developed testing method is significantly high, in this way the authors would like to execute laboratory tests with lower time demand (e.g. particle splitting tests), so relevant statements can be sentenced sooner. The authors would like to combine this splitting test with a full-field 3D shape measurement (ATOS fringe projection system) and/or X-ray measurement technique. The measurement method need to be work out [18, 34, 35, 36, 37, 38, 39, 40, 41, 42].

Beside them field tests are planned in the Hungarian railway lines. The authors would like to collect samples from old railway lines where ballast aggregates have known PSD at time of construction. The actual PSD can be definable and the changing can be determined, too. In case a lot of these kinds of measurements are able to be performed the comparison (not only field samples but the others from laboratory dynamic pulsating tests) can supply valuable results.

In the laboratory measured particle breakage values are much higher than the values in real circumstances in tracks, either in tracks with maintenance (ballast screening) demand. The reason is the only one type of loading form used in laboratory. The authors would like to develop their methodology to be able to assess

the particle degradation more realistic. Tamping machines also break ballast particles, so this kind of effect is needed to be considered in the future research. Other additional dynamic loading effect can't be neglected in sophisticated methods, e.g. surroundings of rail welts, rail joints, as well as switch frogs where higher ballast breakage should be expected [27, 28, 29, 30, 31, 32]. Rubber coated and bitumen stabilised ballast particles hinder the geometric deterioration of railway track and ballast breakage [43, 44, 45], in detailed analysis it can be considered.

DEM simulations with particle flow code software (e.g. Itasca PFC^{3D}) can be useful in the future researches to be able to evaluate particle degradation. With this DEM method the expensive laboratory tests can be saved (if the model is validated with laboratory measurements), influence effect of lots of parameters can be considered, e.g. particle shape, PSD, stone physics, abraded particles, geosynthetic reinforcements, depth of ballast, etc. This method unfortunately very lengthy, and there is just a little chance for good results.

The authors' future aim is to utilize of the results and maybe to adopt these results of the research into national regulations, standards.

This article is the direct continuation of papers [46, 47] that are accepted manuscripts without publishing yet.

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